7.3 Solving Logarithmic/Exponential Equations Notes

Objective: Solve logarithmic equations using properties/rules of logarithms and a calculator

The Principle of Logarithmic Equality

For any logarithmic base, b, and for any x > 0 and y > 0, x = y is equivalent to $\log_b x = \log_b y$. In other words, two expressions are equal if and only if the logarithms of those expressions are equal.

In order to solve logarithmic functions, you will need a combination of the following skills:

- The principle of logarithmic equality
- Properties of logarithms
- Expanding/condensing logarithms
- Change of base formula (calculating log's with a calculator)

****** Always check your solution. Check for extraneous solutions. Remember you cannot take the log/ln of 0 or a negative number

Examples: Solve the following equations. Round to the nearest thousandth if necessary.

1.
$$ln(30x + 2) = ln(-2x + 66)$$

2.
$$\log_4(x-5) = -1$$

3.
$$\ln(x-3) + \ln(x+4) = 3\ln(2)$$

4.
$$50e^{0.035x} = 200$$

5.
$$25^{2x+1} = 144$$