## Math 3 - Trigonometry in Real Life Notes

In this section, we will combine everything we know about trig functions to solve real world problems. Review all the formulas you have learned so far:

Given a Right Triangle $\triangle \mathrm{ABC}$, recall your right triangle trig ratios:


$$
\begin{aligned}
& \text { sine }(\theta)=\sin \theta=\frac{\text { opposite }}{\text { hypotenuse }} \\
& \text { cosine }(\theta)=\cos \theta=\frac{\text { adjacent }}{\text { hypotenuse }} \\
& \text { tangent }(\theta)=\tan \theta=\frac{\text { opposite }}{\text { adjacent }}
\end{aligned}
$$

Given $\triangle A B C$ that is not a right triangle:


| Area of a Triangle |  |
| :--- | :--- |
| Area $=\frac{1}{2} b c(\sin A)$ |  |
| Area $=\frac{1}{2} a c(\sin B)$ |  |
| Area $=\frac{1}{2} a b(\sin C)$ | $\underline{\text { Law of Sines }}$ |
| $\frac{\sin A}{a}=\frac{\sin B}{b}=\frac{\sin C}{c}$ |  |
| $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$ |  |
|  | $a^{2}=b^{2}+c^{2}-2 b c \cos A$ |
| $b^{2}=a^{2}+c^{2}-2 a c \cos B$ |  |
| $c^{2}=a^{2}+b^{2}-2 a b \cos C$ |  |

Other helpful bits of information to recall

- Complimentary angles add up to $90^{\circ}$ (form a right angle)
- Supplementary angles add up to $180^{\circ}$ (form a straight angle or straight line)
- ALL triangles' 3 interior angles add up to $180^{\circ}$
- Word problems are ALWAYS easier when you draw and label a picture

1. Two airplanes leave an airport at the same time on different runways. One flies on a bearing of $\mathrm{N} 57^{\circ} \mathrm{E}$ ( $57^{\circ}$ east of north) at 320 miles per hour. The other airplane flies on a bearing of $\mathrm{S} 23^{\circ} \mathrm{E}\left(23^{\circ}\right.$ east of south) at 310 miles per hour. How far apart will the airplanes be after 1.5 hours?
2. Two ships leave a harbor at the same time. One ship travels on a bearing of $\mathrm{N} 14^{\circ} \mathrm{E}$ at 12 miles per hour. The other ship travels on a bearing of $\mathrm{S} 74^{\circ} \mathrm{W}$ at 9 miles per hour. To the nearest tenth of a mile, how far apart will the ships be after three hours?
3. Two observers are 450 feet apart on opposite sides of a flagpole. The angles of elevation from the observers to the top of the pole are $23^{\circ}$ and $25^{\circ}$. Find the height of the flagpole to the nearest foot.
4. The FCC is attempting to locate an illegal radio station. It sets up two monitoring stations, A and B, with station B 30 miles east of station A. Station A measures the illegal signal from the radio station as coming from a direction of $42^{\circ}$ east of north. Station B measures the signal as coming from a point $40^{\circ}$ west of north. How far is the illegal radio station from monitoring stations A and B ?
